

- b) Kinetic energy calculations, unlike momentum, require converting units to standard units. Also, consider speed.

before collision

$$\begin{array}{cc} \textcircled{1} & \textcircled{2} \\ m_1 = 0.225 \text{ kg} & m_2 = 0.125 \text{ kg} \\ v_1 = 0.300 \text{ m/s} & v_2 = 0.100 \text{ m/s} \end{array}$$

after collision

$$\begin{array}{cc} \textcircled{1} & \textcircled{2} \\ m_1 = 0.225 \text{ kg} & m_2 = 0.125 \text{ kg} \\ v'_1 = 0.222 \text{ m/s} & v'_2 = 0.240 \text{ m/s} \end{array}$$

Kinetic energy of object 1 before

$$\begin{aligned} E_{k1} &= \frac{1}{2} m_1 v_1^2 \\ &= \frac{1}{2} (0.225 \text{ kg})(0.300 \text{ m/s})^2 \\ &= 1.0125 \times 10^{-2} \text{ J} \end{aligned}$$

Kinetic energy of object 2, before

$$\begin{aligned} E_{k2} &= \frac{1}{2} m_2 v_2^2 \\ &= \frac{1}{2} (0.125 \text{ kg})(0.100 \text{ m/s})^2 \\ &= 6.25 \times 10^{-4} \text{ J} \end{aligned}$$

Kinetic energy of object 1, after

$$\begin{aligned} E'_{k1} &= \frac{1}{2} m_1 (v'_1)^2 \\ &= \frac{1}{2} (0.225 \text{ kg})(0.222 \text{ m/s})^2 \\ &= 5.5445 \times 10^{-3} \text{ J} \end{aligned}$$

Kinetic energy of object 2, after

$$\begin{aligned} E'_{k2} &= \frac{1}{2} m_2 (v'_2)^2 \\ &= \frac{1}{2} (0.125 \text{ kg})(0.240 \text{ m/s})^2 \\ &= 3.60 \times 10^{-3} \text{ J} \end{aligned}$$

Total kinetic energy before collision

$$\begin{aligned} &= 1.0125 \times 10^{-2} \text{ J} + 6.25 \times 10^{-4} \text{ J} \\ &= 1.075 \times 10^{-2} \text{ J} \end{aligned}$$

Total kinetic energy after collision

$$\begin{aligned} &= 5.5445 \times 10^{-3} \text{ J} + 3.60 \times 10^{-3} \text{ J} \\ &= 9.1445 \times 10^{-3} \text{ J} \end{aligned}$$

Mechanical (kinetic) energy lost in collision

$$\begin{aligned} &= 1.075 \times 10^{-2} \text{ J} - 9.1445 \times 10^{-3} \text{ J} \\ &= 1.61 \times 10^{-3} \text{ J} \end{aligned}$$

\therefore collision is inelastic.

12. a) before collision



Consider right as positive

$$\begin{array}{cc} m_1 = 10.0 \text{ g} & m_2 = 30.0 \text{ g} \\ \bar{v}_1 = 20.0 \text{ cm/s} & \bar{v}_2 = 0 \\ \bar{p}_1 = 200 \text{ g} \cdot \text{cm/s} & \bar{p}_2 = 0 \end{array}$$

$$\therefore \bar{p}_{\text{before}} = \bar{p}_1 + \bar{p}_2 = 200 \text{ g} \cdot \text{cm/s}$$

after collision



$$\begin{array}{cc} m_1 = 10.0 \text{ g} & m_2 = 30 \text{ g} \\ \bar{v}'_1 = -6.0 \text{ cm/s} & \bar{v}'_2 = ? \\ \bar{p}'_1 = -60 \text{ g} \cdot \text{cm/s} & \bar{p}'_2 = ? \\ \bar{p}_{\text{sys(after)}} = \bar{p}_{\text{sys(before)}} = 200 \text{ g} \cdot \text{cm/s} \\ \bar{p}'_2 = 200 \text{ g} \cdot \text{cm/s} - (-60 \text{ g} \cdot \text{cm/s}) \\ &= 260 \text{ g} \cdot \text{cm/s} \end{array}$$

$$\begin{aligned} \bar{v}'_2 &= \frac{\bar{p}'_2}{m} \\ &= \frac{260 \text{ g} \cdot \text{cm/s}}{30.0 \text{ g}} \\ &= 8.67 \text{ cm/s right} \end{aligned}$$

- b) Kinetic energy calculations, unlike momentum, require converting units to standard units.

before collision

$$\begin{array}{cc} \textcircled{1} & \textcircled{2} \\ m_1 = 0.0100 \text{ kg} & m_2 = 0.0300 \text{ kg} \\ v_1 = 0.200 \text{ m/s} & v_2 = 0 \end{array}$$

after collision

$$\begin{array}{cc} \textcircled{1} & \textcircled{2} \\ m_1 = 0.0100 \text{ kg} & m_2 = 0.0300 \text{ kg} \\ v'_1 = -0.060 \text{ m/s} & v'_2 = 0.0867 \text{ m/s} \end{array}$$